

Adveksi Mundur

Untuk memudahkan penjabaran, maka didefinisikan variabel sbb:

$$\begin{aligned} C_{i,n+1} &= C(i,n+1) \\ C_{i,n} &= C(i,n) \\ C_{i-1,n} &= C(i-1,n) \end{aligned}$$

$$\text{Adveksi} := (C_{i,n+1} - C_{i,n})/\Delta t + U (C_{i,n} - C_{i-1,n})/\Delta x$$

$$\text{Taylor} := \left\{ \begin{aligned} C_{i,n+1} &\rightarrow C_{i,n} + \partial C/\partial t \Delta t + \partial^2 C/\partial t^2 \Delta t^2/2, \\ C_{i-1,n} &\rightarrow C_{i,n} - \partial C/\partial x \Delta x + \partial^2 C/\partial x^2 \Delta x^2/2 \end{aligned} \right\}$$

$$\text{Identitas} := \partial^2 C/\partial t^2 \rightarrow U^2 \partial^2 C/\partial x^2$$

$$\text{AdveksiNew1} := \text{Adveksi} / \text{Taylor} / \text{Identitas}$$

$$\text{AdveksiNew2} = \text{ExpandAll}[\text{AdveksiNew1}]$$

$$\partial C/\partial t + U \partial C/\partial x + \frac{U^2 \partial^2 C/\partial x^2 \Delta t}{2} - \frac{U \partial^2 C/\partial x^2 \Delta x}{2}$$

$$\begin{aligned} \text{AdveksiBaru} &:= \partial C/\partial t + U \partial C/\partial x - K_n \partial^2 C/\partial x^2; \\ K_n &:= U \Delta x/2 - U^2 \Delta t/2 \end{aligned}$$

$$\text{Selisih} = \text{Simplify}[(\text{AdveksiBaru} - \text{AdveksiNew2}) / \text{Identitas}]$$

0

Jika didefinisikan $Cr = U\Delta t/\Delta x$, maka kecepatan dapat ditulis sebagai:

$$\text{Identitas3} := U \rightarrow Cr \Delta x/\Delta t$$

sehingga K_n dapat ditulis sebagai:

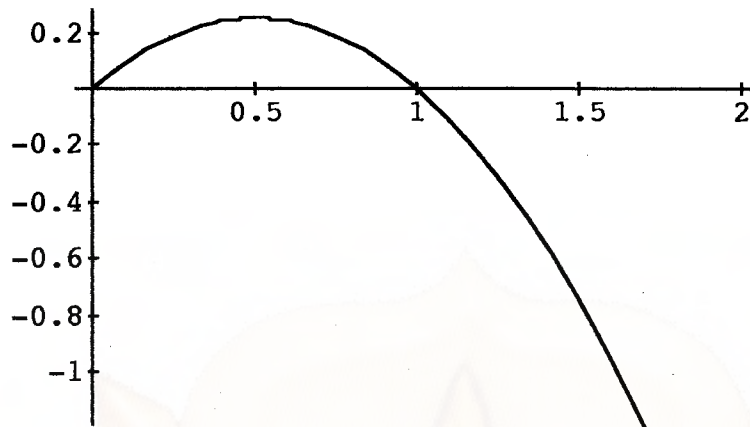
$$K_{nbaru} := \text{Simplify}[K_n / \text{Identitas3}]; K_{nbaru}$$

$$\frac{-((-1 + Cr) Cr \Delta x)}{2 \Delta t}$$

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Plot [Knbaru/. { $\Delta x \rightarrow 1, \Delta t \rightarrow 1/2$ }, {Cr, 0, 2}]



-Graphics-

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